

Addition and Subtraction

Parent Workshop - How we teach addition and subtraction so that they really understand



Aims of workshop

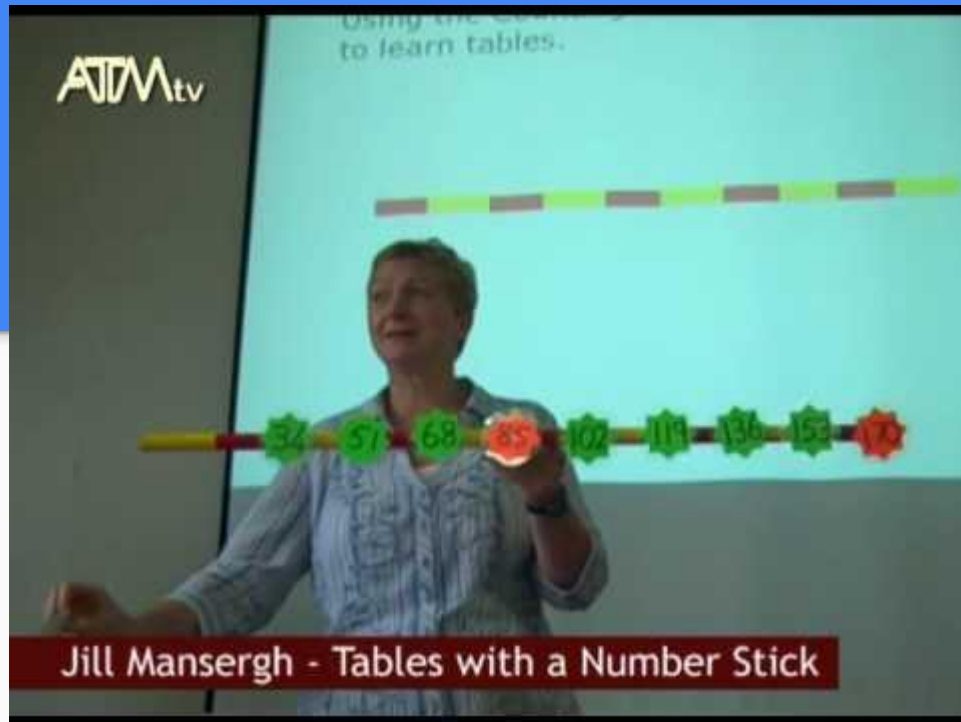
- Counting
- Written Methods for addition and subtraction
- Mental Methods for addition and subtraction
- Reasoning and problem solving with addition and subtraction
- Growth Mindset

The national curriculum for mathematics aims to ensure that all pupils:

- become fluent in the fundamentals of mathematics, including through varied and frequent practice with increasingly complex problems over time, so that pupils develop conceptual understanding and the ability to recall and apply knowledge rapidly and accurately.
- reason mathematically by following a line of enquiry, conjecturing relationships and generalisations, and developing an argument, justification or proof using mathematical language
- can solve problems by applying their mathematics to a variety of routine and non-routine problems with increasing sophistication, including breaking down problems into a series of simpler steps and persevering in seeking solutions.

Mathematics is an interconnected subject in which pupils need to be able to move fluently between representations of mathematical ideas. ... pupils should make rich connections across mathematical ideas to develop fluency, mathematical reasoning and competence in solving increasingly sophisticated problems. They should also apply their mathematical knowledge to science and other subjects. National Curriculum 2014

Counting



<https://www.youtube.com/watch?v=yXdHGBfoqfw>

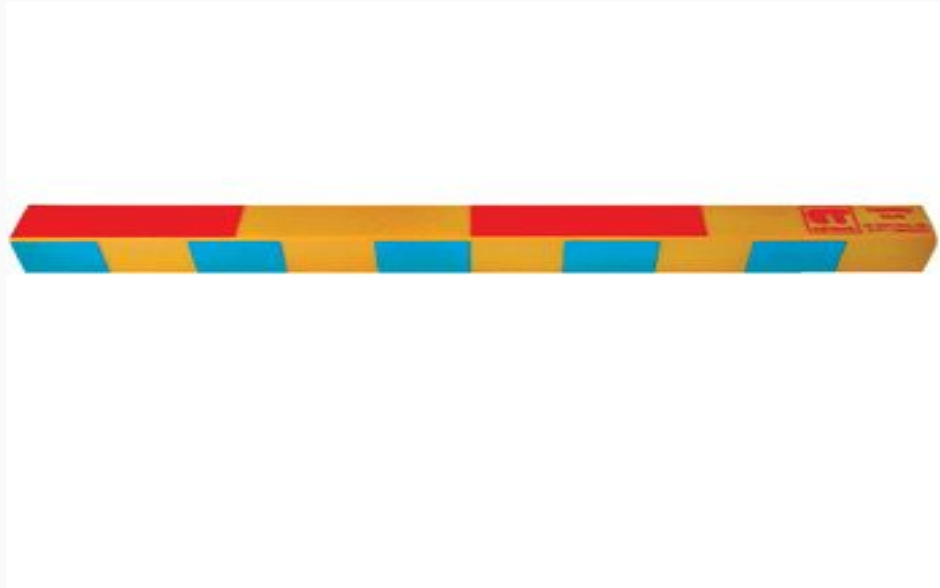
Counting in the new curriculum

- count in steps of 2, 3, and 5 from 0, and in tens from any number, forward and backward
- count from 0 in multiples of 4, 8, 50 and 100; find 10 or 100 more or less than a given number
- count in multiples of 6, 7, 9, 25 and 1000
- count forwards or backwards in steps of powers of 10 for any given number up to 1 000 000
- interpret negative numbers in context, count forwards and backwards with positive and negative whole numbers, including through zero

Counting in the new curriculum

- count in steps of 2, 3, and 5 from 0, and in tens from any number, forward and backward - **year 2**
- count from 0 in multiples of 4, 8, 50 and 100; find 10 or 100 more or less than a given number - **year 3**
- count in multiples of 6, 7, 9, 25 and 1000 - **year 4**
- count forwards or backwards in steps of powers of 10 for any given number up to 1 000 000 - **year 5**
- interpret negative numbers in context, count forwards and backwards with positive and negative whole numbers, including through zero - **year 5**

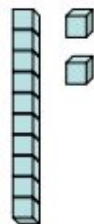
Counting Activities



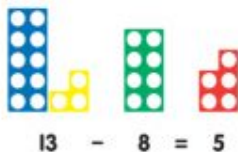
Communicating
Mathematically



Active/concrete



Building visual images



13 - 8

Abstract

12 + 19



Pattern
Spotting

Written Methods

$$\begin{array}{r} 5189 \\ + 3128 \\ \hline 8317 \\ \hline 11 \end{array}$$

$$\begin{array}{r} 51.89 \\ + 3.128 \\ \hline 55.018 \\ \hline 11 \end{array}$$

$$\begin{array}{r} 2 13 11 1 \\ 1\cancel{3} 4\cancel{2} 3 \\ - 12678 \\ \hline 745 \\ \hline \hline \end{array}$$

How do we get to here?

Year 2 Expectations - Addition

- Partition numbers in different ways - e.g. $23 = 20 + 3$ or $10 + 13$
- add and subtract including:
 - a two-digit number and ones
 - a two-digit number and tens
 - two two-digit numbers
 - three one-digit numbers

They will be used to using practical resources to support their adding and subtracting

bead string

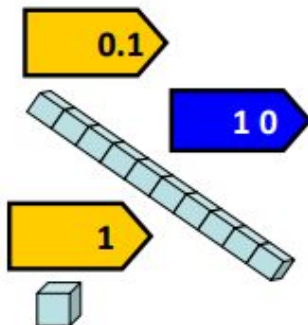


count stick



place value apparatus

Hundreds 200s	Tens 10s	Units/Ones 1s



Multilink



place value counters

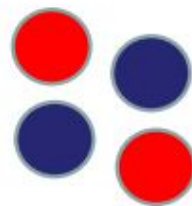


Cuisenaire

Numicon



number line



double sided counters












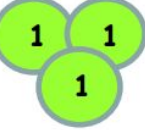



1	2	3	4	5	6	7	8	9	10
11	12	13	14	15	16	17	18	19	20
21	22	23	24	25	26	27	28	29	30
31	32	33	34	35	36	37	38	39	40
41	42	43	44	45	46	47	48	49	50
51	52	53	54	55	56	57	58	59	60
61	62	63	64	65	66	67	68	69	70
71	72	73	74	75	76	77	78	79	80
81	82	83	84	85	86	87	88	89	90
91	92	93	94	95	96	97	98	99	100
101	102	103	104	105	106	107	108	109	110
111	112	113	114	115	116	117	118	119	120
121	122	123	124	125	126	127	128	129	130
131	132	133	134	135	136	137	138	139	140
141	142	143	144	145	146	147	148	149	150
151	152	153	154	155	156	157	158	159	160
161	162	163	164	165	166	167	168	169	170
171	172	173	174	175	176	177	178	179	180
181	182	183	184	185	186	187	188	189	190
191	192	193	194	195	196	197	198	199	200

1	2	3	4	5	6	7	8	9	10
11	12	13	14	15	16	17	18	19	20
21	22	23	24	25	26	27	28	29	30
31	32	33	34	35	36	37	38	39	40
41	42	43	44	45	46	47	48	49	50
51	52	53	54	55	56	57	58	59	60
61	62	63	64	65	66	67	68	69	70
71	72	73	74	75	76	77	78	79	80
81	82	83	84	85	86	87	88	89	90
91	92	93	94	95	96	97	98	99	100

number grids
100 and 200

$$\begin{array}{r}
 40 + 1 \\
 + 20 + 8 \\
 \hline
 60 + 9 = 69
 \end{array}$$

$$\begin{array}{r}
 40 + 3 \\
 + 20 + 8 \\
 \hline
 70 + 1 \\
 \hline
 10 = 71
 \end{array}$$

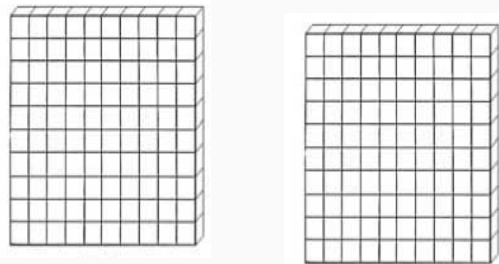
Hundreds  100s	Tens  10s	Units/Ones  1s
		
		
		
		

The children would use manipulatives alongside the methods to understand how they work!

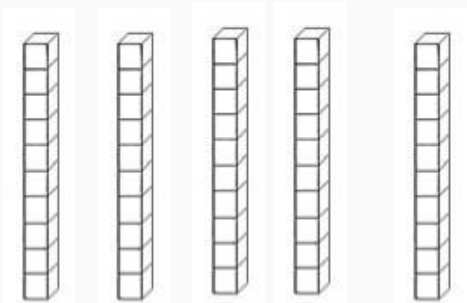
Expanded recording

$$\begin{array}{r} 100 + 40 + 1 \\ + 100 + 20 + 8 \\ \hline 200 + 60 + 9 = 269 \end{array}$$

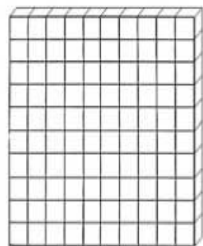
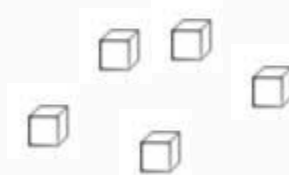
Hundreds
100s



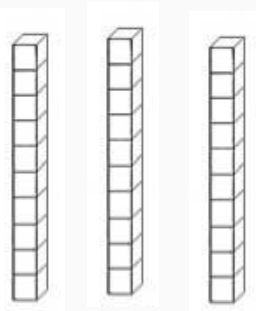
Tens
10s



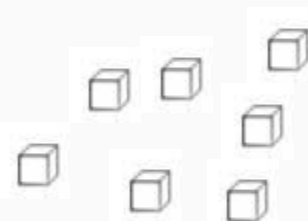
Units/ ones
10s



300

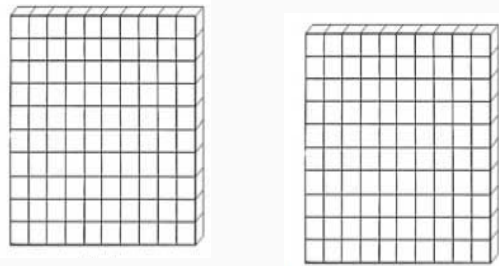


80

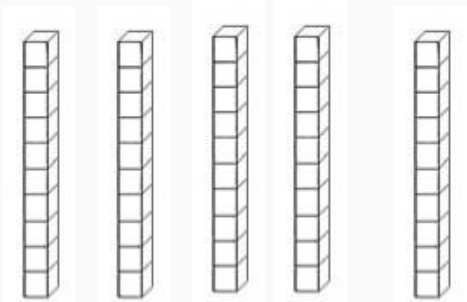


12

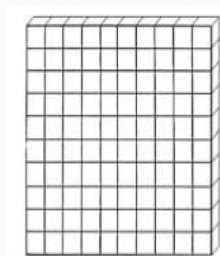
Hundreds
100s



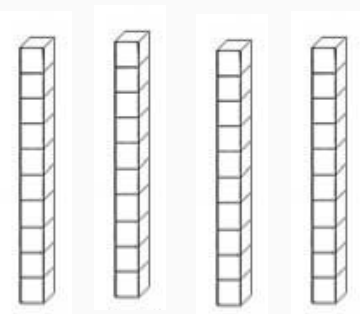
Tens
10s



Units/ ones
10s



300



90



2

Your turn

Have a go at:

- $247 + 145 = \underline{\hspace{2cm}}$

Try to use the dienes to show what you are doing!

Moving on...

$$\begin{array}{r} 2141 \\ + 1128 \\ \hline 3269 \\ \hline \end{array}$$

Column addition (no exchanging)

$$\begin{array}{r} 21.41 \\ + 1.12 \\ \hline 0.35 \\ \hline 22.88 \\ \hline \end{array}$$

$$\begin{array}{r} 5189 \\ + 3128 \\ \hline 8317 \\ \hline 11 \end{array}$$

Column addition (with exchanging)

$$\begin{array}{r} 51.89 \\ + 3.128 \\ \hline 55.018 \\ \hline 11 \end{array}$$

Challenge - building in *reasoning*

Find the missing numbers in the addition.

$$\begin{array}{r} \square 4 \\ + 2 \square \\ \hline \end{array}$$

$$62$$

The children need to really understand how to use the method to find the missing numbers

Spot the mistake

- Find the errors in the calculations and correct them to find the right answer.

Calculation	Error	Correct solution
$\begin{array}{r} 256 \\ + 347 \\ \hline 2907 \end{array}$		
$\begin{array}{r} 63 \\ - 38 \\ \hline 35 \end{array}$		

The children need to spot errors and explain where the mistake is!

Again, they need to really understand the method!

Multiple solutions

The answer to the addition is 201. All the digits used are either 1 or 9. Fill in the boxes.

$$201 = \square\square + \square\square + \square\square$$

Is there more than 1 solution?

Have they found all of the solutions?

The children need to *convince, justify* and *explain!*

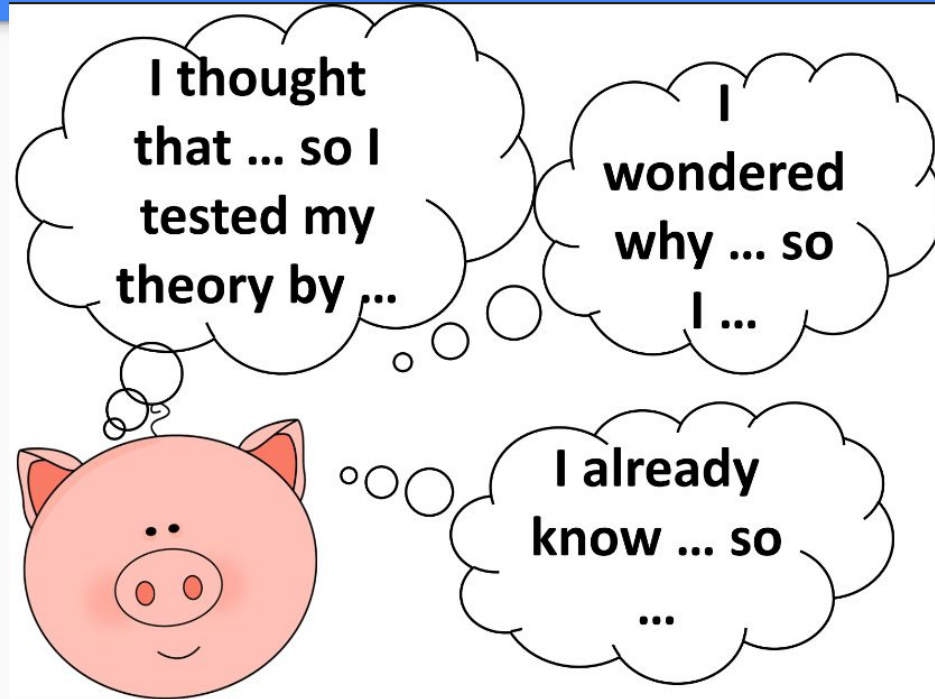
Reasoning

You have been given some reasoning tasks from years 3 to 6.

Can you work out which colour is which?

Find a problem from your child's year group to solve!

Supporting reasoning



Subtraction

no exchange

$$\boxed{68 - 23}$$

$$60 \quad 8$$

$$\begin{array}{r} \text{—} \\ 20 \quad 3 \end{array}$$

$$40 + 5 = 45$$

with exchange

$$\boxed{63 - 28}$$

$$\cancel{50} \quad 60 \quad 10 + 3$$

$$\begin{array}{r} \text{—} \\ 20 \quad 8 \end{array}$$

$$30 + 5 = 35$$

Moving on...

$$148 - 121$$

$$100 \quad 40 \quad 8$$

$$\begin{array}{r} 100 \quad 40 \quad 8 \\ - 100 \quad 20 \quad 1 \\ \hline \end{array}$$

$$0 + 20 + 7 = 27$$

*Column subtraction
(no exchange)*

$$\begin{array}{r} 148 \\ - 121 \\ \hline 27 \\ \hline \end{array}$$

And on...

Column subtraction (with exchange)

723 - 317

$$\begin{array}{r} 7^1 \cancel{2}^1 3 \\ - 317 \\ \hline 406 \end{array}$$

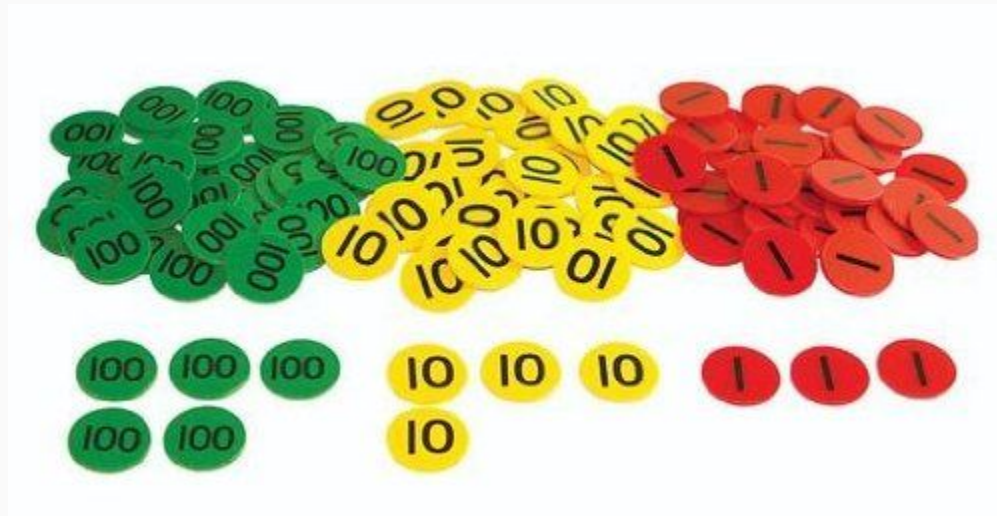
723 - 367

$$\begin{array}{r} 6 \cancel{7}^{11} \cancel{2}^1 3 \\ - 367 \\ \hline 356 \end{array}$$

$$\begin{array}{r} 6 \cancel{7}^{11} \cancel{2}^1 3 \\ - \pounds 3.67 \\ \hline \pounds 3.56 \end{array}$$

With Place Value Counters

Can you solve $4023 - 2918$ using place value counters?



And on!

Column subtraction (no exchanging)

$$\begin{array}{r} 13548 \\ - 12128 \\ \hline 1420 \end{array}$$

Column subtraction
(with exchanging)

$$\begin{array}{r} \overset{2}{1} \overset{13}{3} \overset{11}{4} \overset{1}{2} 3 \\ - 12678 \\ \hline 745 \end{array}$$

Playing Games

The aim of the game is to get as close to 1000 as possible. Each player rolls their dice, and places the number in their calculation grid. Once both grids are full, subtract the 2 numbers and see who is the closest!



Problem Solving

$$\begin{array}{r} \\ - \\ \hline \end{array}$$

Can you work out what the missing numbers would be?

9

Mr and Mrs Jones are saving for a holiday.

Mr Jones has saved £742

Mrs Jones has saved £1359

The holiday costs £3415

How much **more** do they need to save?

Show
your
method

£

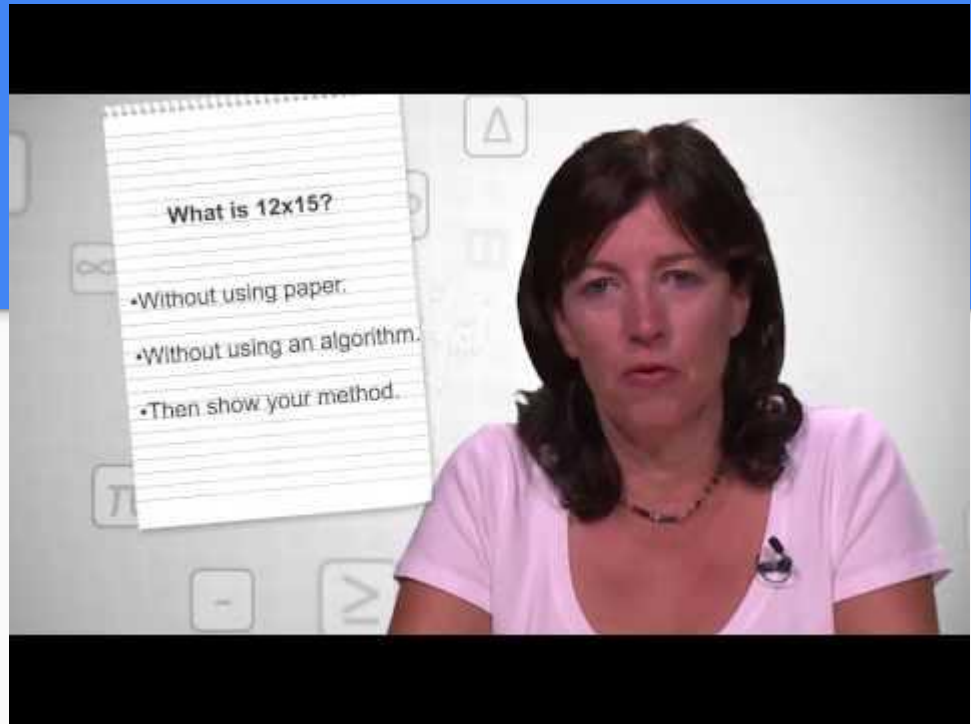
1 0 0 0 0 0

9 9 9 9 9

-

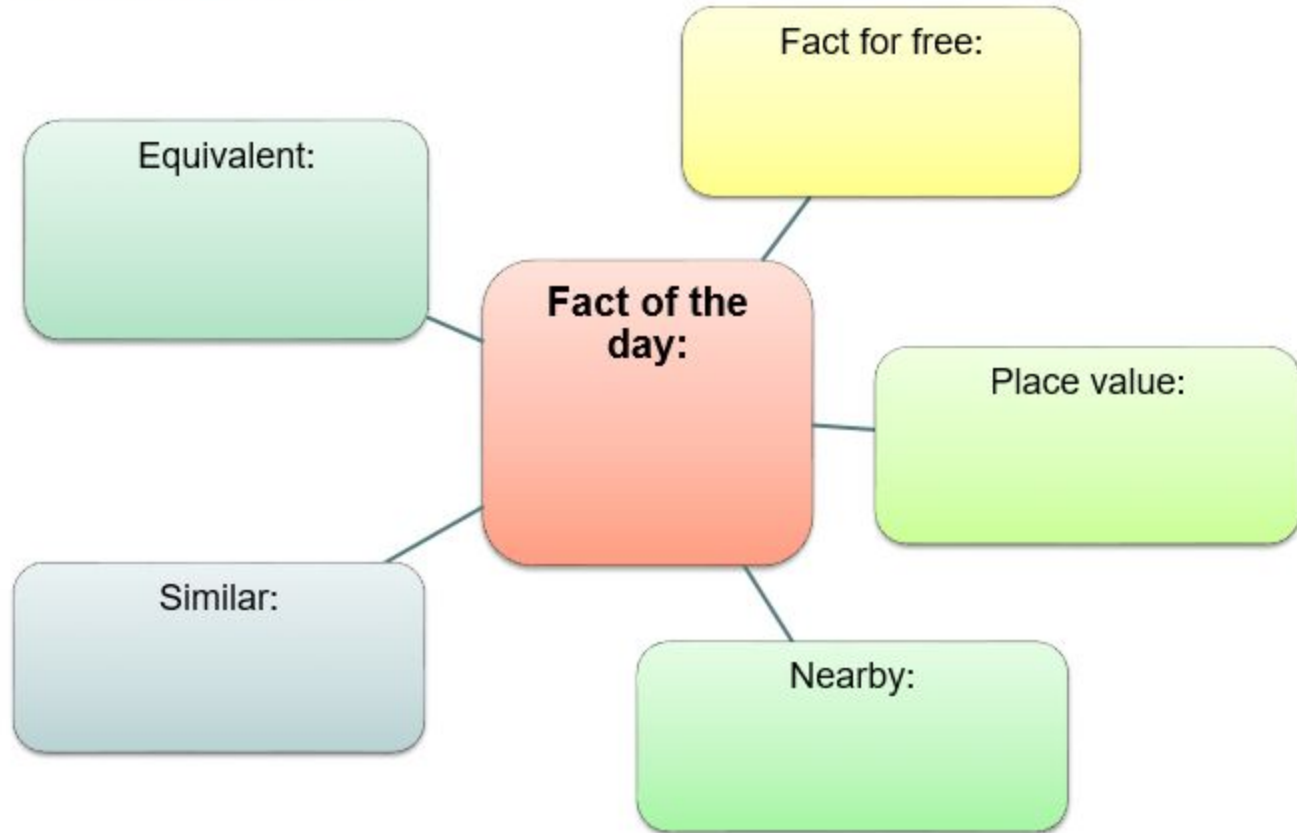


Number Talks



<https://www.youtube.com/watch?v=yXNG6GKFhQM>

Deriving facts



Fact for free:

$$170 - 80 = 90$$

Equivalent:

$$110 + 60 = 170$$

Fact of the day:

$$80 + 90 = 170$$

Place value:

$$8,000 + 9,000 = 17,000$$

$$0.8 + 0.9 = 1.7$$

Nearby:

$$82 + 88 = 170$$

Growth Mindset



<https://www.youtube.com/watch?v=3e9a4Hjc9SM>

Fixed mind-set vs Growth mind-set



An individual's learning is shaped by whether they believe their intelligence is fixed or can be changed:

- If you have a fixed mind set you believe that your abilities are fixed and that you can either do mathematics or you can't
- If you have a growth mind set you believe that you can learn and become better at mathematics
- Children who have a fixed mind set are at a significant disadvantage compared to children who have a growth mind set

Negative portrayal in the media



“Age is just a number
and maths was never my
thing.”

L'Oréal Paris advert changed 2015

Product
withdrawn by EE
January 2016
after many
complaints



DAVID & GOLIATH
BLONDE PHONE
SOCK - IM TOO
PRETTY TO DO
MATHS

£4.00

ADD TO BASKET

Damaging maths mindset holding pupils back

30% wrongly believe that maths is a skill you are born with, rather than a skill that can be learnt.

“The cultural acceptability of saying ‘I can’t do maths’”

An international study (OECD) ranked the UK 26th out of 65 countries for maths ability.

Children in the UK the equivalent of 3 years behind peers in Shanghai.